## Model error correction with data assimilation and machine learning

Alban Farchi<sup>\*1</sup>, Marc Bocquet<sup>2</sup>, Massimo Bonavita<sup>3</sup>, and Patrick Laloyaux<sup>3</sup>

<sup>1</sup>CEREA – École des Ponts ParisTech (ENPC), EDF Recherche et Développement – 6-8 avenue Blaise-Pascal, Cité Descartes, Champs-sur-Marne, France

<sup>2</sup>CEREA – École des Ponts ParisTech (ENPC), EDF Recherche et Développement – 6-8 avenue Blaise

Pascal, Cité Descartes, Champs-sur-Marne, France

<sup>3</sup>ECMWF – Reading, United Kingdom

## Abstract

The idea of using machine learning (ML) methods to reconstruct the dynamics of a system is the topic of recent studies in the geosciences, in which the key output is a surrogate model meant to emulate the dynamical model. In order to treat sparse and noisy observations in a rigorous way, ML can be combined to data assimilation (DA). This yields a class of iterative methods in which, at each iteration a DA step assimilates the observations, and alternates with a ML step to learn the underlying dynamics of the DA analysis.

This framework can be used to correct the error of an existent, physical model. The resulting surrogate model is hybrid, with a physical and a statistical part. In practice, the correction can be added as an integrated term (i.e. in the model resolvent) or directly inside the tendencies of the physical model. The resolvent correction is easy to implement but is not suited for short-term predictions. The tendency correction is more technical, in particular it requires the adjoint of the physical model, but also more flexible and can be used for any prediction.

In this presentation, we start by a proof of concept for the use of joint DA and ML tools to correct model error. We use the resolvent correction with simple neural networks to correct the error of a two-dimensional, two layer quasi-geostrophic model. We then illustrate the difference between the resolvent and the tendency correction with the two-scale Lorenz system. Finally, we show that the tendency correction opens the possibility to make online model error correction, i.e. improving the model progressively as new observations become available. We compare online and offline learning using the same twin experiment with the two-scale Lorenz system.

Keywords: data assimilation, machine learning, model error, neural ntworks

\*Speaker